# 17EC52

# Fifth Semester B.E. Degree Examination, June/July 2023 **Digital Signal Processing**

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

Compute the N-point DFT of the sequence, x(n) = an,  $0 \le n \le N-1$ . (06 Marks) 1

Obtain the relationship between DFT and discrete-time Fourier transform of aperiodic (06 Marks) signals.

State and prove the following properties related to N-point DFT:

ii) Multiplication of two DFTs. i) Linearity

(08 Marks)

Compute the 8-point DFT of the sequence,  $x[n] = \{1, 1, 1, 1, 0, 0, 0, 0\}$ . (08 Marks) 2

Compute the N-point DFT of the following:

i) 
$$x_1(n) = \cos\left(\frac{2\pi n}{N}\right), \ 0 \le n \le N-1$$
 ii)  $x_2(n) = 1, \ 0 \le n \le N-1$ . (12 Marks)

# Module-2

The 8-point DFT of a length – 8 complex sequence: 3

V(n) = x(n) + ih(n) is given by;

$$V(0) = -2 + j3$$
,  $V(1) = 1 + j5$ ,  $V(2) = -4 + j7$ 

$$V(3) = 2 + j6$$
,  $V(4) = -1-j3$ ,  $V(5) = 4-j$ 

V(6) = 3 + j8, V(7) = j6

Without computing IDFT of V(K) determine the 8-point DFTs of the sequences x(n) and (08 Marks) h(n).

b. Discuss the filtering of long data sequences using overlap-save method. (06 Marks)

c. Let x(n) be a finite length sequence with X(k) = (0, 1 + j, 1, 1 - j). Using the properties of DFT, find DFTs of the following sequences:

i) 
$$x_1(n) = e^{j\pi/2n} x(n)$$

ii) 
$$x_2(n) = \cos\left(\frac{\pi}{2}n\right)x(n)$$

ii) 
$$x_2(n) = \cos\left(\frac{\pi}{2}n\right)x(n)$$
 iii)  $x_3(n) = x((n-1))_4$ . (06 Marks)

a. Why do we adopt FFT algorithms for the computation of N-point DFT. (04 Marks)

b. Perform x(n) \* h(n), for the sequences x(n) and h(n) given below using overlap-add method: h(n) = (1, 1, 1)

x(n) = (1, 2, 0, -3, 4, 2, -1, 1, -2, 3, 2, 1, -3).

Consider the initial data blocks size to be 6.

(08 Marks)

c. Prove the following:

i) DFT
$$\{x(n)W_N^{-\ell n}\}=X((K-\ell))_N$$

DFT
$$\{x(n)W_N^{-\ell n}\}=X((K-\ell))_N$$
 ii)  $\sum_{n=0}^{N-1}|x(n)|^2=\frac{1}{N}\sum_{K=0}^{N-1}|x(k)|^2$ .

(08 Marks)

# Module-3

Compute the 8-point DFT of the sequence, 5

 $x(n) = \{1, 1, 1, 1, -1, -1, -1, -1\}$ , using DIT-FFT algorithm.

(08 Marks)

Derive the second order Goertzel filter which can be used for computation of DFT samples. (08 Marks)

- c. In the computation of N-point DFT using FFT algorithms, how many
  - Complex multiplications are involved?
  - ii) Complex additions are involved?
  - Real registers are used? iii)
  - Butterflies (basic building blocks) are used? iv)

(04 Marks)

#### OR

Develop DIF-FFT algorithm for the computation of 8-point DFT. 6

(08 Marks)

Write an explanatory note on Chirp-z transform.

(07 Marks)

Find the 4-point real sequence x(n), if its 4-point DFT samples are X(0) = 6, X(1) = -2 + j2, X(2) = -2. Use DIF-FFT algorithm.

(05 Marks)

# Module-4

a. An LTI system is characterized by the difference equation: 7

y(n) - 0.5y(n-2) - 2y(n-3) = 1.5 x(n-2).Realize the system in i) Direct form – I ii) Direct form – II structures.

(08 Marks)

- Derive the expressions for order and cut-off frequency related to analog low-pass (08 Marks) Butterworth filter.
- An analog filter has the transfer function;  $H_a(s) = \frac{1}{s+2}$ . Transform  $H_a(s)$  to a digital filter, H(z), using impulse invariance technique. Consider the sampling rate to be 2Hz.

### OR

A digital lowpass filter is required to meet the following specifications: 8 Monotonic passband and stopband.

> -3.01dB cutoff frequency of  $0.5\pi$  rad. And, stopband attenuation of atleast 15dB at  $0.75\pi$  rad. Find the system function H(z) using Bilinear transformation. (12 Marks)

Obtain a parallel realization for the transfer function H(z) given below.

$$H(z) = \frac{8 - 4z^{-1} + 11z^{-2} - 2z^{-3}}{\left(1 - \frac{1}{4}z^{-1}\right)\left(1 - z^{-1} + \frac{1}{2}z^{-2}\right)}$$

(08 Marks)

#### Module-5

A filter is to be designed with the following desired frequency response:

$$H_{d}(w) = \begin{cases} 0, & -\pi/4 < w < \pi/4 \\ e^{-j2w}, & \pi/4 < |w| < \pi \end{cases}$$

Use a rectangular window to design the related FIR filter and find its frequency response. (10 Marks)

- b. Write the relevant equations and stop band attenuations obtained from following windows:
  - i) Rectangular
- ii) Hanning
- iii) Hamming.

(06 Marks)

Realize on FIR filter with system function,  $H(z) = 1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2} + \frac{1}{9}z^{-3}$ . (04 Marks)

Realize the linear-phase FIR filter having the following impulse response: 10

> $h(n) = \delta(n) + \frac{1}{4}\delta(n-1) - \frac{1}{8}\delta(n-2) + \frac{1}{4}\delta(n-3) + \delta(n-4).$ (06 Marks)

- A three-stage FIR lattice structure has the following coefficients:  $K_1 = 0.65$ ,  $K_2 = -0.34$  and  $K_3 = 0.8$ . Evaluate its impulse response by tracing a unit impulse  $\delta(n)$  at its input through the lattice structure. Also, draw its direct form-I structure.
- The frequency response of an FIR filter is given by  $H(w) = e^{-j2w} (1 + 1.8\cos 2w + 1.2\cos w)$ . Determine impulse response coefficients of FIR filter. (04 Marks)

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